

# CHANNELING IN DIRECT DARK MATTER DETECTION

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*Based on work in progress with G. Gelmini and P. Gondolo*

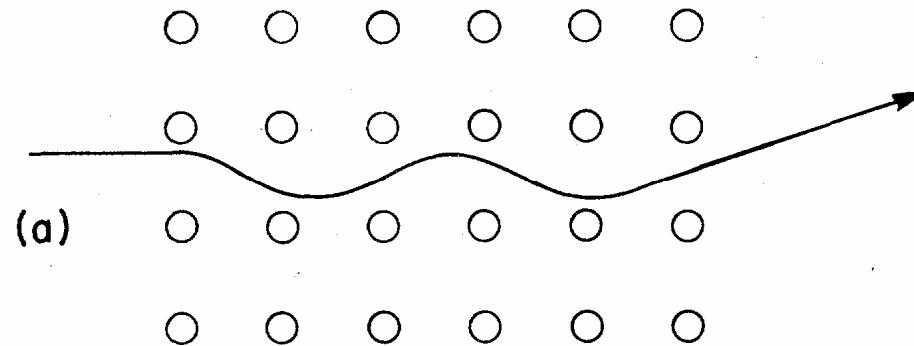
# Outline

- Channeling and blocking in crystals
- Channeling effect in direct dark matter detection
- Basic idea for daily modulation
- Channeling fraction for
  - ▣ Incoming particles
  - ▣ Recoiling nuclei
- Conclusions and future prospects

# Channeling and Blocking in Crystals

## (a) Channeling:

If an *incident* ion is along the symmetry axis or planes of the crystal, it will have a series of small-angle scatterings which will maintain it in the open channels. The ion will penetrate much further into the crystal than in other directions.

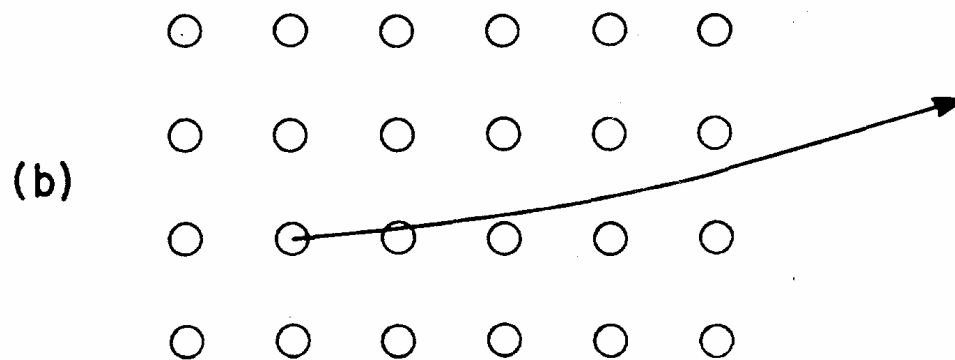


From D. Gemmell 1974, *Rev. Mod. Phys.* 46, 129

# Channeling and Blocking in Crystals

## (b) Blocking:

If an ion *originating* in the lattice sites is along the symmetry axis or planes, there is a *reduction* in the flux of the ion when it exits the crystal creating a “blocking dip”.



*From D. Gemmell 1974, Rev. Mod. Phys. 46, 129*

# Channeling and Blocking in Crystals

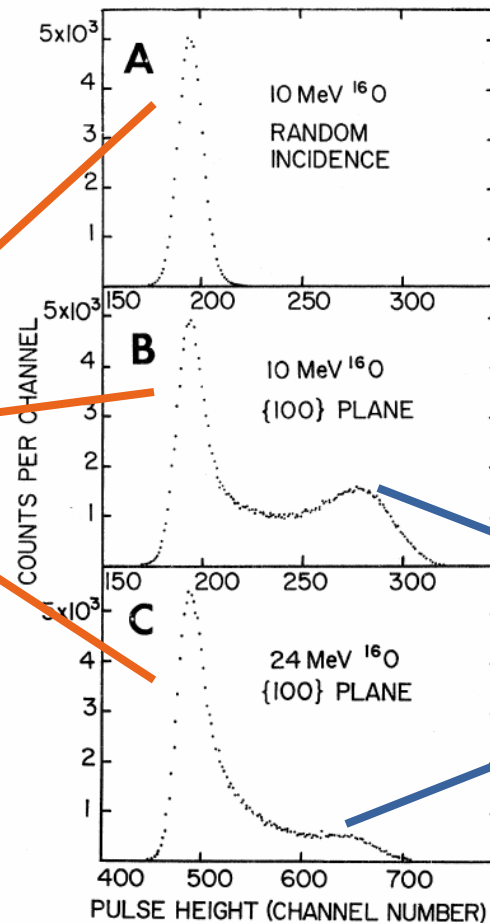
- Channeling and blocking in crystals is used in:
  - crystallography
  - studies of lattice disorder
  - ion implantation
  - finding the location of dopant and impurity atoms
  - studies of surfaces and interfaces
  - measurement of short nuclear lifetimes
  - production of polarized beams
  - etc.

# Observation of Channeling Effect in NaI (TI)

- Channeling effect in NaI (TI) was first observed in 1973 by Altman et al. (*Phys. Rev. B7, 1743*).
- They observed that the scintillation output of a monochromatic 10 MeV  $^{16}\text{O}$  beam through NaI (TI) scintillator has two peaks:
  - peak with **lower** scintillation output:  
*non-channeled* ions
  - peak with a **higher** scintillation output:  
*channeled* ions

# Observation of Channeling Effect in NaI (TI)

Not  
channeled



Channeled

FIG. 2. (a) Pulse-height spectrum from 10-MeV  $^{16}\text{O}$  on NaI(Tl) for incidence along a random direction. (b) Pulse-height spectrum from 10-MeV  $^{16}\text{O}$  along a {100} plane. (c) Pulse-height spectrum from 24-MeV  $^{16}\text{O}$  along a {100} plane. A light guide was used in all cases.

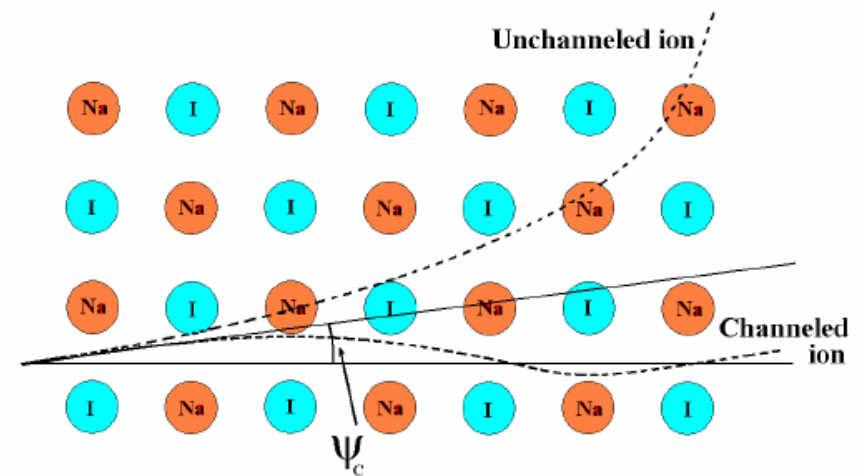
*Altman et al. Phys.  
Rev. B7, 1743*

# Channeling Effect in Direct DM Detection

- The importance of channeling effect for direct DM detection was pointed out for NaI by the DAMA collaboration (*DAMA- Eur. Phys. J. C53, 205-2313, 2008*).

$$E_{\text{measured}} = QE_{\text{recoil}}$$

- When Na or I recoils move along a channel, their quenching factor is  $Q = 1$  instead of  $Q_{Na} = 0.3$  and  $Q_I = 0.09$ , since they give their energy to electrons.

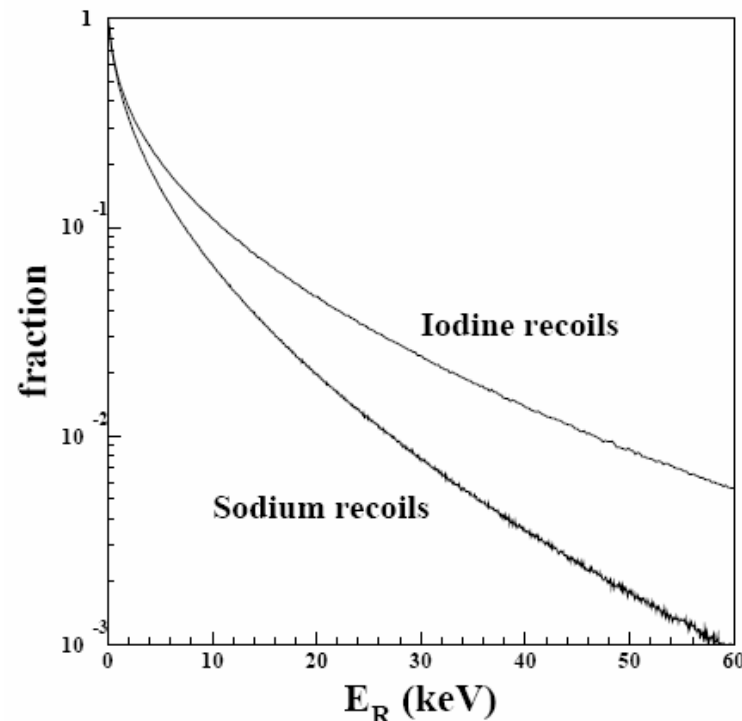


*DAMA- Eur. Phys. J. C53, 205-2313, 2008*



# Channeling Effect in Direct DM Detection

- The DAMA collaboration found that the fraction of channeled recoils is large for low recoil energies.



**DAMA- *Eur. Phys. J. C53, 205-2313, 2008***

# Basic Idea for Daily Modulation

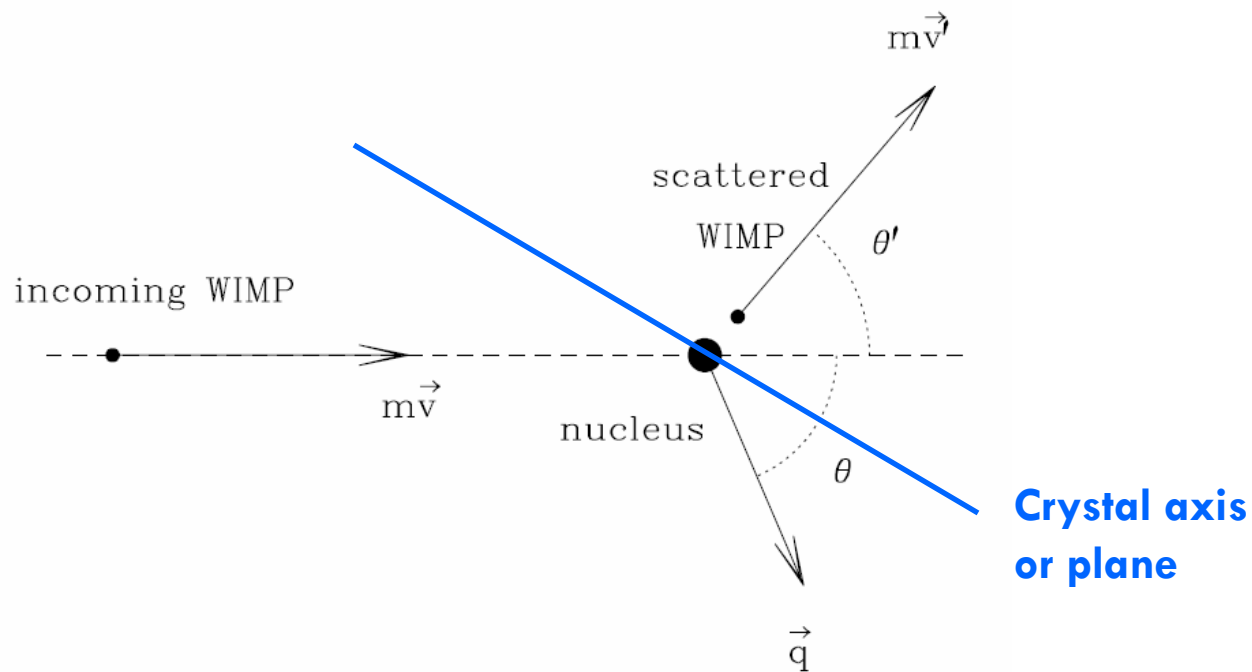
- The WIMP wind comes preferentially from one direction, due to the motion of the Earth with respect to the galaxy.
- When that direction is aligned with a channel, the scintillation or ionization output is larger ( $Q = 1$  instead of  $< 1$ ).
- Earth's daily rotation makes the WIMP wind change direction with respect to the crystal.
- This produces a daily modulation in the “measured” recoil energy (as if the quenching factor were modulated).

# Basic Idea for Daily Modulation

- If this daily modulation is measured it would have no background → Ideal for DM search.
- Avignone et al. mention a modulation amplitude of  $\sim 25\%$  as a somewhat simplistic estimate.  
*Avignone, Creswick, Nussinov 2008 (arXiv:0807.3758)*
- We set out to do a better calculation and in the process understand channeling and blocking for DM detection with analytic models.
- Our results are preliminary and our work is in progress.

# What we need:

- Consider the WIMP-nucleus elastic collision for a WIMP of mass  $m$  and a nucleus of mass  $M$ .




*From Gondolo 2002, Phys. Rev. D 66, 103513*

# What we need:

- We need to determine the probability  $p(E, E_R, \hat{\mathbf{q}})$  that an energy  $E$  is measured when the recoil is in the direction  $\hat{\mathbf{q}}$  with energy  $E_R$ .
- The recoil nucleus can either be channeled or not channeled:

$$p(E, E_R, \hat{\mathbf{q}}) = \underbrace{\chi(E_R, \hat{\mathbf{q}})\delta(E - E_R)}_{\text{Channeled}} + \underbrace{[1 - \chi(E_R, \hat{\mathbf{q}})]\delta(E - QE_R)}_{\text{Not Channeled}}$$



where  $\chi(E_R, \hat{\mathbf{q}})$  is the fraction of channeled nuclei with recoil energy  $E_R$  in direction  $\hat{\mathbf{q}}$ .

# Modeling of Channeling

- Our calculations are based on classical analytic models developed in the 1960's and 70's, in particular Lindhard's model (*Lindhard 1965, Komaki & Fujimoto 1970, Dearnaley 1973, Gemmell 1974, Appleton & Foti 1977*).
- We use the continuum string or plane model, in which the screened Thomas-Fermi potential is averaged over a direction parallel to the row or plane.
- Only one row or one plane is considered.
- In the direction perpendicular to the row or plane, the “transverse energy”  $E_{\perp} = E \sin^2 \psi + U$  , is conserved.

# Our Calculations

- ❑ Compute the channeling fraction for:
  - ❑ Incoming particles
  - ❑ Recoiling nuclei

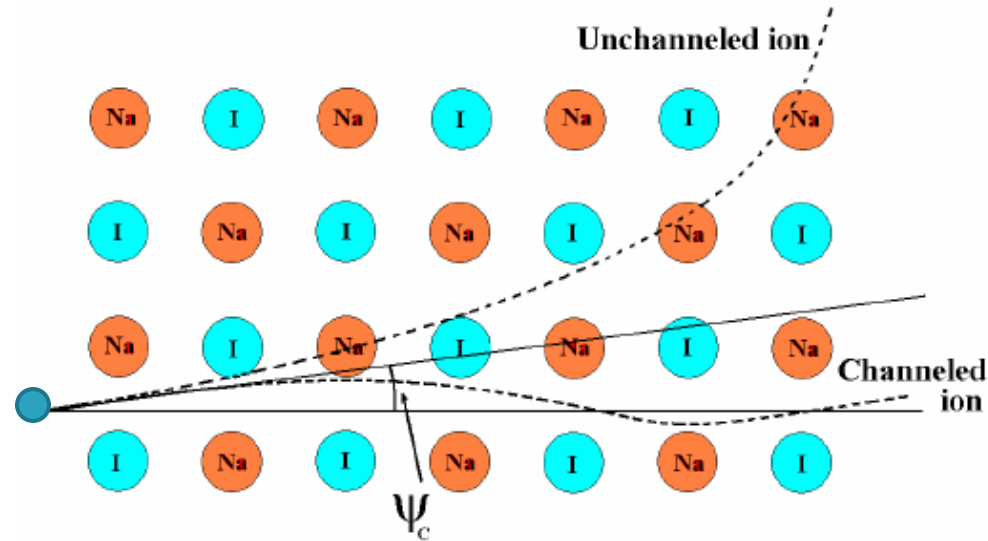
# Our Calculations

- ❑ Compute the channeling fraction for:
  - ❑ Incoming particles
  - ❑ Recoiling nuclei



# Channeling of Incoming Particles

- Low energy incident ions are considered to be channeled if they are incident upon a string or plane of atoms at some angle  $\psi$  smaller than a critical angle  $\psi_c$  (Lindhard 1965).



*DAMA- Eur. Phys. J. C53, 205-2313, 2008*

# Channeling Fraction of Incoming Particles

- We will integrate the channeling probability over direction to find the total fraction of channeled nuclei:

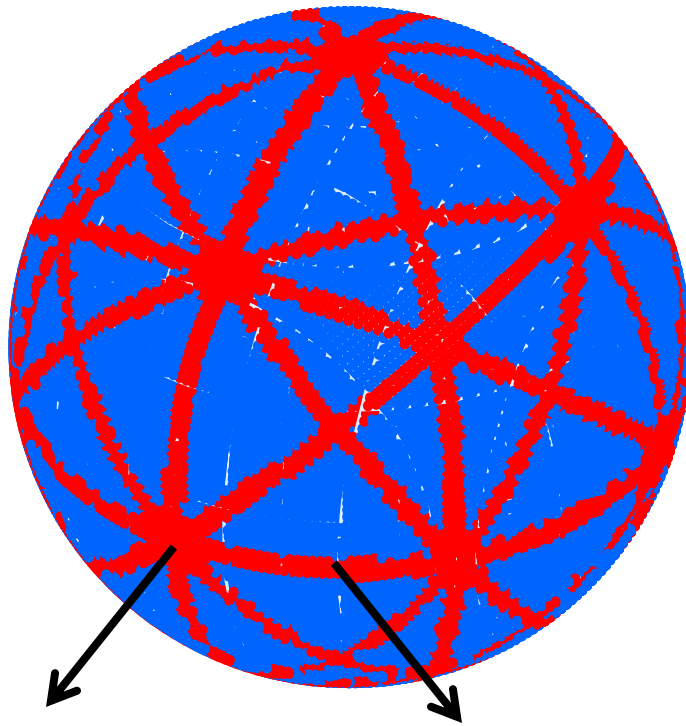
$$P(E) = \frac{1}{4\pi} \int \chi(E, \hat{\mathbf{q}}) d\Omega_q$$

where  $d\Omega_q$  is an infinitesimal solid angle around  $\hat{\mathbf{q}}$

- We used the Hierarchical Equal Area isoLatitude Pixalization (HEALPix) method to compute the integral.

# Fraction of channeled Na

Using the HEALPix pixalization of the sphere for incident energy of 50 keV



Axial channel

Planar channel

For each **axial** channel:

$$\chi_{\text{axial}}(E, \psi) = 1$$

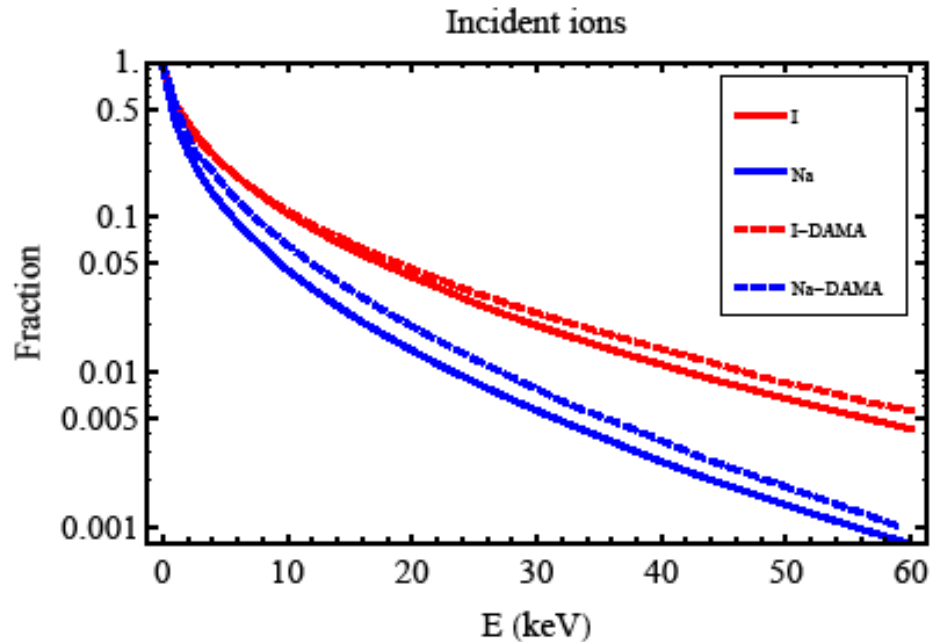
$$\text{if } \psi < \psi_c^{\text{axial}}$$

For each **planar** channel:

$$\chi_{\text{planar}}(E, \psi) = 1$$

$$\text{if } \psi < \psi_c^{\text{planar}}$$

# Channeling Fraction of Incoming Particles



- We agree with DAMA results to a good approximation.
- Our result is based on analytic calculations with basic assumptions, whereas DAMA is using Monte Carlo.

# Our Calculations

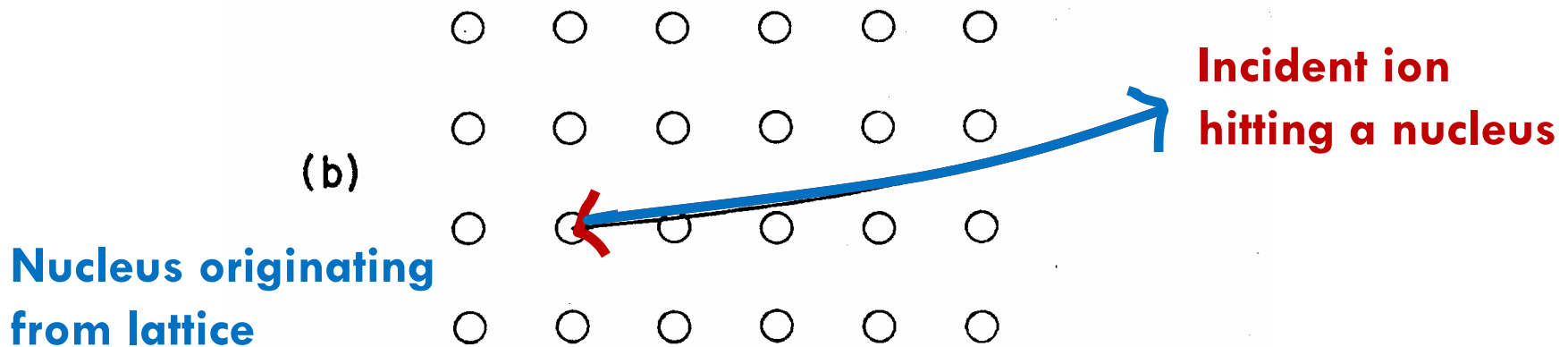
- ❑ Compute the channeling fraction for:
  - ❑ Incoming particles
  - ❑ Recoiling nuclei

# Our Calculations

- ❑ Compute the channeling fraction for:
  - ❑ Incoming particles
  - ❑ Recoiling nuclei

# Channeling of Recoiling Nuclei

- Recoiling nuclei start at or close to the lattice sites
- In a perfect lattice no recoil would be channeled (“rule of reversibility”).



- However, there are channeled recoils due to **lattice vibrations** as already understood in the 70's.

# Channeling of Recoiling Nuclei

- For a given  $E_R$  and  $\psi$ , the condition for channeling is given by:

$$E_R \sin^2 \psi + U(r_i) < U(r_c)$$

initial distance

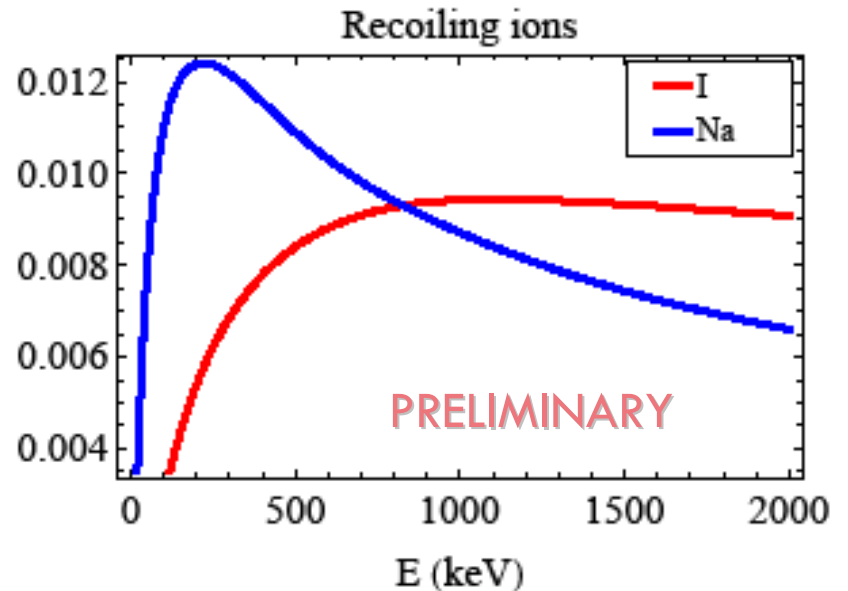
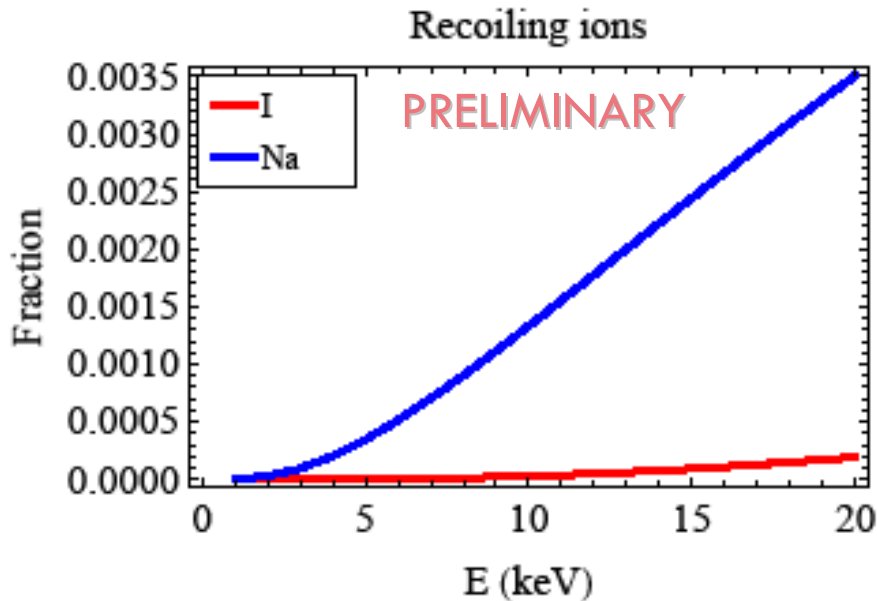
Smallest possible minimum  
distance of approach

- The distribution function of the emitting atom due to thermal vibrations can be represented by a Gaussian.
- The fraction of channeled nuclei recoiling at angle  $\psi$  with the axis is equal to

$$\chi_{\text{axial}}(E_R, \psi) = \int_{r_{i,\min}}^{\infty} dr g(r)$$



# Fraction of Recoils that are Channeled



- This result now differs from DAMA results.
- These are upper bounds to what we can expect to be the true fraction.

# Preliminary Conclusions

- Channeling in crystalline detectors can lead to a daily modulation in a WIMP signal.
- Channeling of recoiling nuclei and incoming particles have different mechanisms. We were able to reproduce DAMA results for incident ions, but for recoiling nuclei the channeling fraction is much smaller.
- Small channeling fractions would mean small daily modulation amplitudes for the SHM.
- Daily modulation amplitudes strongly depend on the velocity dispersion of the WIMP, and would be larger for dark halo components with a smaller velocity dispersion.

# Future Prospects

- We are writing a paper about the channeling fractions for NaI, Ge and Si.
- We will evaluate the daily modulations for NaI, Ge and Si to obtain more accurate results.
- Analytic results may not be enough, and we may collaborate with other groups to carry out sophisticated Monte Carlo simulations to confirm our results.

**Thank You!**







Additional

# Channeling of Recoiling Nuclei

- We want to find the probability that the particle will go in the 1<sup>st</sup> or 2<sup>nd</sup> or ... or 26<sup>th</sup> channel.
- The total channeling prob. for each energy and direction is computed using a recursion of the addition rule in probability theory over all axial and planar channels:

$$P_{n+1} = P_n + \Delta P_n, \quad P_0 = P_{\text{axial}}, \quad P_{26} = P_{\text{axial}} + P_{\text{planar}},$$

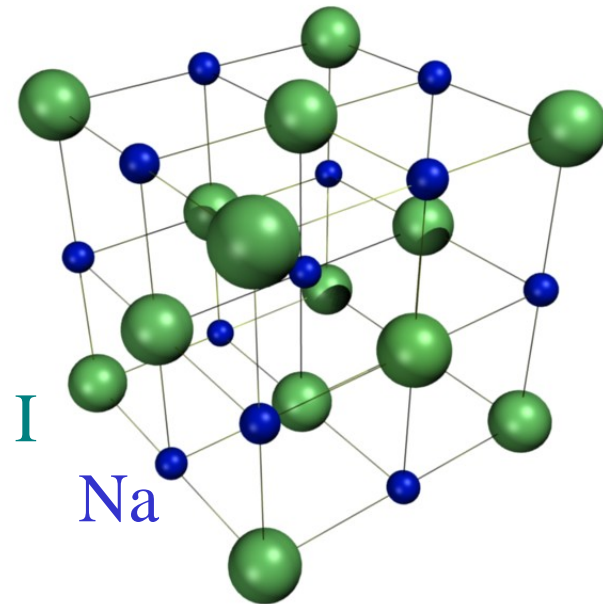
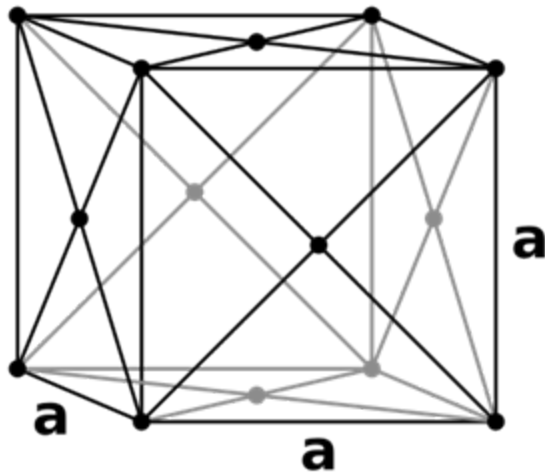
- We can continue this recursive computation until we find the probability that the particle will go into either of the 26 channels:

$$P_{\text{channel}} = P_{\text{axial}} + P_{\text{planar}}, \quad P_{\text{axial}} = P_{\text{axial}} + P_{\text{planar}},$$



# Structure of NaI

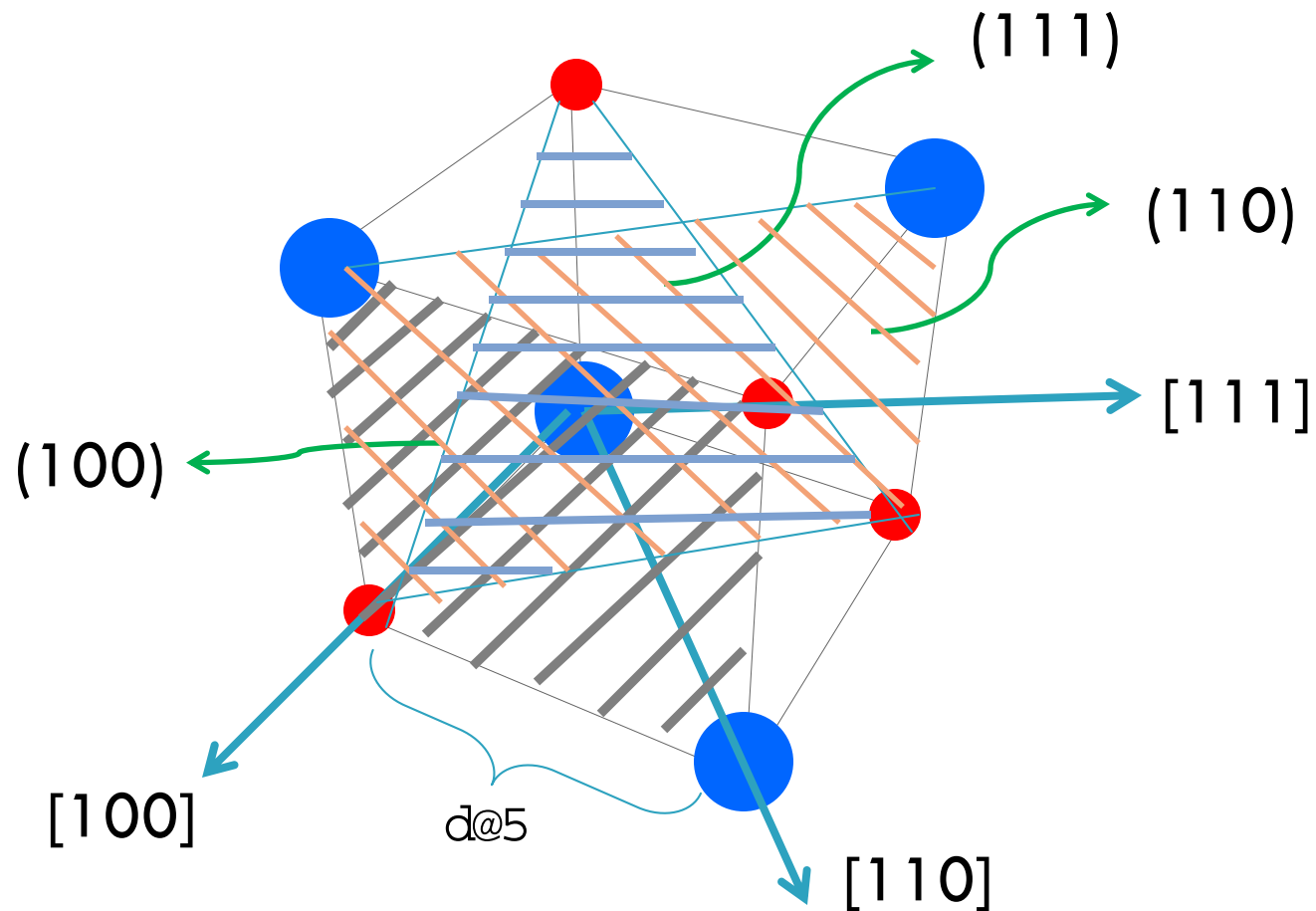
- NaI is a diatomic compound which is composed of two interpenetrating f.c.c. sublattices



<http://commons.wikimedia.org/wiki/File:Nacl-structure.jpg>

# Structure of NaI

- Unit cell of NaI crystal:



# Structure of NaI

- We will only consider the lower index crystallographic axis and planes:

- For axial channeling we consider:

$$\langle 100 \rangle, \langle 110 \rangle, \langle 111 \rangle$$

- For planar channeling we consider:

$$\{100\}, \{110\}, \{111\}$$

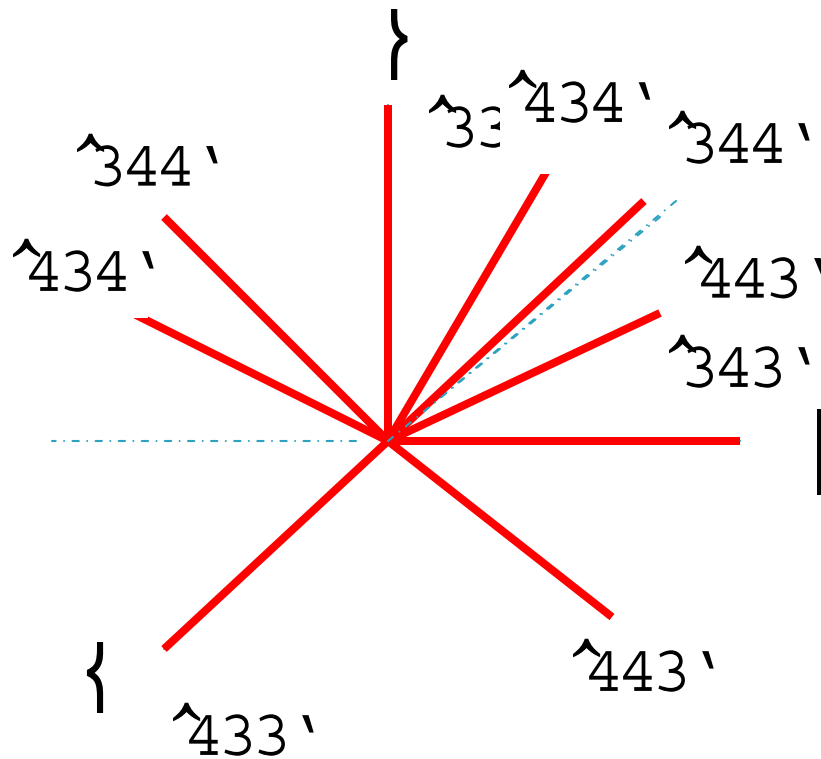
- We have a total of **26** channels:

- 13 Axial

- 13 planar: perpendicular to the axial channels

# Structure of NaI

□ 13 axial channels:



3

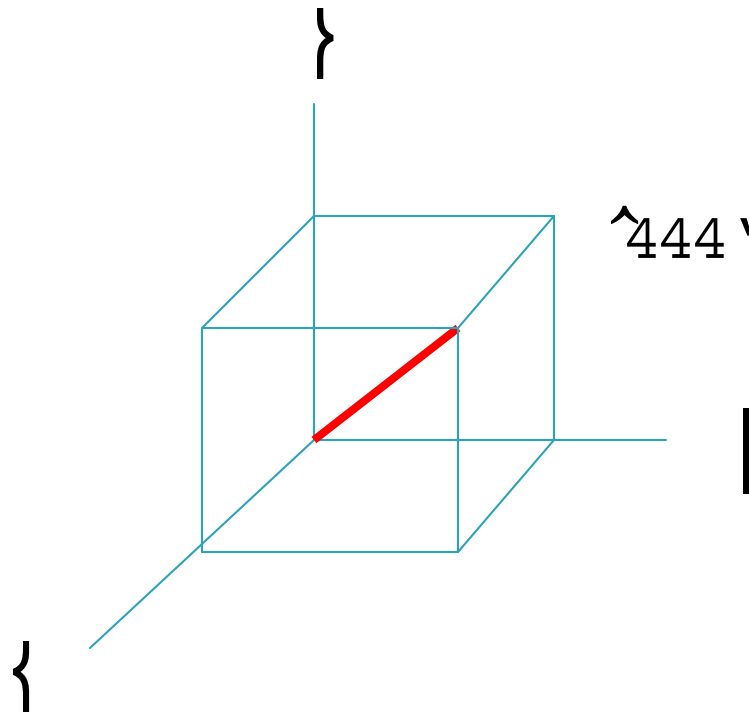


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# Structure of NaI

- 13 axial channels:



3

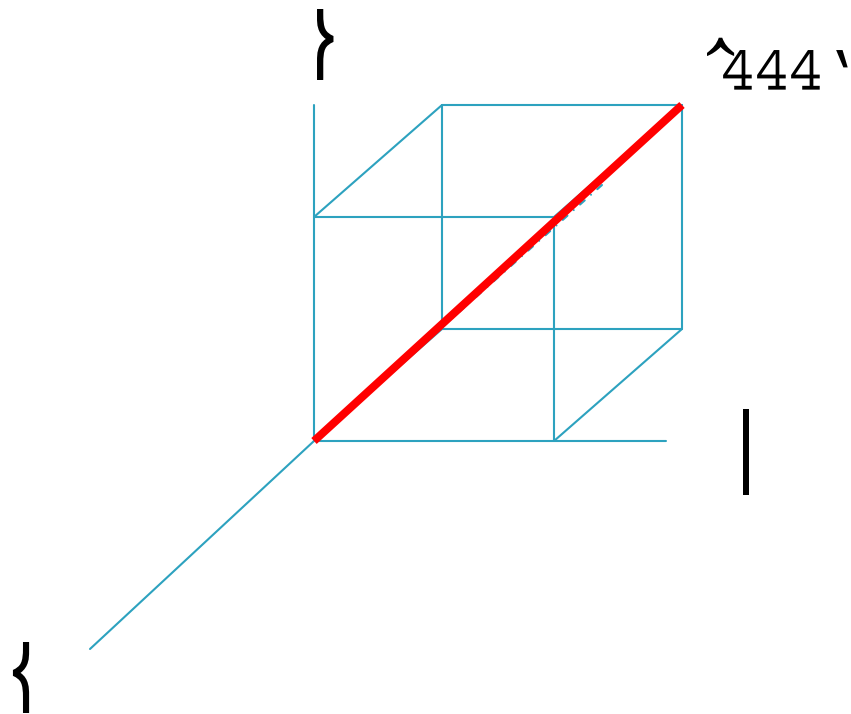


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# Structure of NaI

- 13 axial channels:



3

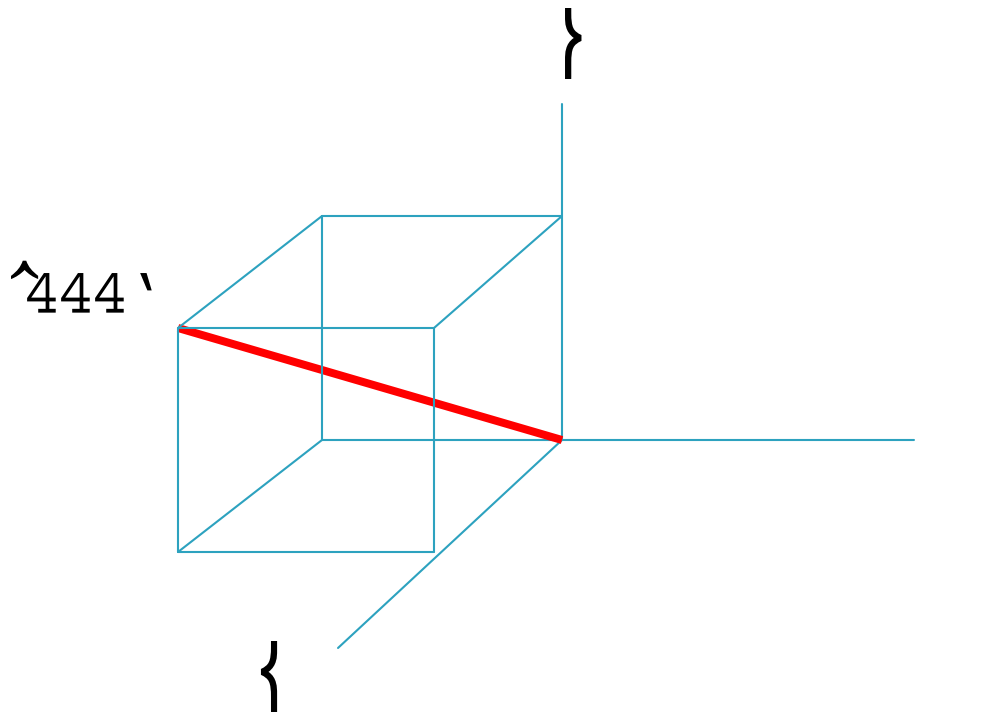


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# Structure of NaI

□ 13 axial channels:



3



6



# Structure of NaI

□ 13 axial channels:

