

EXAM 4

Name: _____ Student ID #: _____

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A 3.00 kg mass is attached to a spring ($k = 52.0 \text{ N/m}$) that is hanging vertically from a fixed support. The mass is moved to a position 0.800 m lower than the unstretched position of the end of the spring. The spring is then released and the mass-spring system executes SHM. Take the 0.800 m of the mass as the reference location for its gravitational PE.

A. [6 pts.] What is the equilibrium position of the mass-spring system?

$$mg = kx_{RQ} \quad x_{RQ} = \frac{mg}{k} = \frac{(3 \text{ kg})(9.8 \text{ m/s}^2)}{52.0 \text{ N/m}}$$

$$x_{RQ} = 0.565 \text{ m}$$

B. [6 pts.] What is the amplitude of the SHM the mass-spring system executes?

$$\text{AMPLITUDE } (A) = 0.800 \text{ m} - 0.565 \text{ m}$$

$$A = 0.235 \text{ m}$$

C. [6 pts.] What is the period of the oscillation of this system?

$$T = 2\pi \sqrt{\frac{m}{k}} = 2\pi \sqrt{\frac{3 \text{ kg}}{52 \text{ N/m}}}$$

$$T = 1.51 \text{ s}$$

D. [6 pts.] What is the total mechanical energy of the mass-spring system at the moment the mass is released?

$$E = \frac{1}{2} k x_{\text{max}}^2 = (.5)(52 \text{ N/m})(.8 \text{ m})^2$$

$$E = 16.6 \text{ J}$$

E. [12 pts.] What are (i) the KE of the mass and (ii) the speed of the mass when the spring is at its equilibrium position?

$$v = v_{\text{max}} = \omega A = \sqrt{\frac{k}{m}} A = \sqrt{\frac{52 \text{ N/m}}{3 \text{ kg}}} (.235 \text{ m})$$

$$v_{\text{max}} = 0.978 \text{ m/s}$$

$$KE = KE_{\text{max}} = \frac{1}{2} m v_{\text{max}}^2 = (.5)(3 \text{ kg})(0.978 \text{ m/s})^2$$

$$KE_{\text{max}} = 1.44 \text{ J}$$