

FIRST MIDTERM

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REPORT ALL NUMBERS TO THREE SIGNIFICANT FIGURES!

Use the conversion constants and data given on the front page.

- (a) A lithium-7 nucleus has 3 protons and 4 neutrons. Calculate the force between a lithium nucleus and an electron 3.00×10^{-11} m apart.

$$F = \frac{k q_1 q_2}{r^2} ; q_1 = 3e ; q_2 = -e ; F = \frac{9 \cdot 10^9 \cdot 3 \cdot (1.6 \cdot 10^{-19})^2}{(3 \cdot 10^{-11})^2} = 7.68 \cdot 10^{-7} \text{ N}$$

(attractive)

- (b) Calculate the electric field (in N/C) at a distance of 4.00×10^{-9} m from a lithium nucleus.

$$E = \frac{kq}{r^2} = \frac{9 \cdot 10^9 \cdot 3 \cdot 1.6 \cdot 10^{-19}}{(4 \cdot 10^{-9})^2} = 2.70 \cdot 10^8 \frac{\text{N}}{\text{C}}$$

- (c) A conducting sphere of radius 1.50×10^{-3} m has a positive charge of 1.75×10^{-11} C. Determine the electric field at a distance of 3.30 m from the center of the sphere.

$$d > R \Rightarrow E = \frac{kq}{d^2} = \frac{9 \cdot 10^9 \cdot 1.75 \cdot 10^{-11}}{(3.3)^2} = 1.45 \cdot 10^{-2} \frac{\text{N}}{\text{C}}$$

- (d) For the expression $1/(x-a)^{5/2}$, where $a \ll x$, calculate completely the term in a^3 using the binomial expansion.

$$(x-a)^{-5/2} = x^{-5/2} \left(1 - \frac{a}{x}\right)^{-5/2} = x^{-5/2} \left(1 - \frac{5}{2} \frac{a}{x} + \frac{5}{2} \frac{7}{2} \frac{1}{2!} \frac{a^2}{x^2} - \frac{5}{2} \frac{7}{2} \frac{9}{3!} \frac{a^3}{x^3} + \dots\right)$$

term in a^3 : $\left(-\frac{5}{2} \cdot \frac{7}{2} \cdot \frac{9}{3!} \frac{1}{x^3}\right) x^{-5/2} = -6.56 \frac{a^3}{x^{11/2}}$

- (e) An electron is accelerated from rest in a uniform electric field of 4.67 N/C. Find the speed of the electron after it has traveled 3.25 cm.

$$F = ma = qE \quad a = \frac{qE}{m} ; \quad v^2 = 2ad$$

$$v = (2ad)^{1/2} = \left(\frac{2qEd}{m}\right)^{1/2} = \left(\frac{2 \cdot 1.6 \cdot 10^{-19} \cdot 4.67 \cdot 0.0325}{9.11 \cdot 10^{-31}}\right)^{1/2} = 2.31 \cdot 10^5 \frac{\text{m}}{\text{s}}$$