

FIRST MIDTERM

3

Name: Solutions

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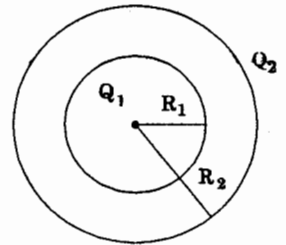
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SHOW ALL WORK!!!!

REPORT ALL NUMBERS TO THREE SIGNIFICANT FIGURES!

Use the conversion constants and data given on the front page.

A uniformly charged sphere of a nonconductor has a radius R_1 and charge Q_1 . It is enclosed in a concentric thin metal spherical shell whose radius is R_2 . ($R_2 > R_1$.) The metal shell has a net total charge Q_2 .



- (a) Calculate the electric field a distance 47.0 cm from the common center of the two spheres. (Numerical answer including sign.)
- (b) Calculate the electric field a distance of 13.5 cm from the common center. (Numerical answer including signs.)
- (c) Calculate the electric field a distance 3.00 cm from the common center. (Numerical answer including sign.)

$Q_1 = -375 \mu\text{C}$; $Q_2 = +172 \mu\text{C}$
 $R_1 = 12.0 \text{ cm}$; $R_2 = 30.0 \text{ cm}$

$$(a) E = \frac{k(Q_1 + Q_2)}{r^2} = \frac{(8.99 \times 10^9 \text{ Nm}^2/\text{C}^2)(-375 \times 10^{-6} + 172 \times 10^{-6} \text{ C})}{(0.47 \text{ m})^2} = \boxed{-8.26 \times 10^6 \text{ N/C}}$$

$$(b) E = \frac{kQ_1}{r^2} = \frac{(8.99 \times 10^9 \text{ Nm}^2/\text{C}^2)(-375 \times 10^{-6} \text{ C})}{(0.135 \text{ m})^2} = \boxed{-1.85 \times 10^8 \text{ N/C}}$$

$$(c) E = \frac{kQ_1 r}{R_1^3} = \frac{(8.99 \times 10^9 \text{ Nm}^2/\text{C}^2)(-375 \times 10^{-6} \text{ C})(0.03 \text{ m})}{(0.12 \text{ m})^3} = \boxed{-5.85 \times 10^7 \text{ N/C}}$$

(equation for part (c) may be derived directly from Gauss' Law)