

FIFTH MIDTERM

3

Name: _____

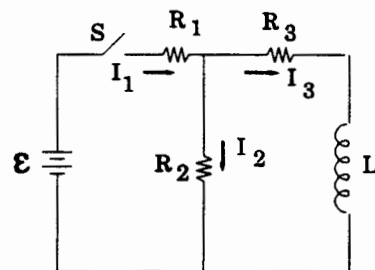
Discussion Instructor (circle): Billeter Blake Gillman Herring

Student ID #: _____

SHOW ALL WORK!!!!
REPORT ALL NUMBERS TO THREE SIGNIFICANT FIGURES!
Use the conversion constants and data given on the front page.

In the circuit shown the switch is closed at $t = 0$ after being open for a long time.

- 5 (a) Find the current in the inductor at $t = \infty$.
 5 (b) Calculate the current in the inductor after 1.25 time constants have elapsed from $t = 0$.
 5 (c) The switch is opened after being closed for 1.25 time constants in (a). Calculate the time constant for the decay of the current in the inductor.
 10 (d) Calculate the time constant for the growth of the current in the inductor with the switch closed. You must develop the differential equation governing the current as function of time. For convenience in grading use the branch current labels and directions given in the drawing. No shortcuts from other classes.



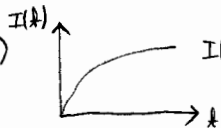
$\epsilon = 225 \text{ V}, R_1 = 7,500 \Omega, R_2 = 12,500 \Omega, R_3 = 12,500 \Omega, L = 5.35 \text{ mH}$

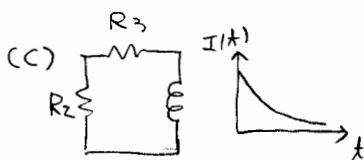
(a) $t = \infty$ inductor acts like a wire.

$$R_{23} = \frac{R_2 R_3}{R_2 + R_3} = 6250, \quad R_{eq} = R_1 + R_{23} = 13750, \quad I = \frac{\epsilon}{R_{eq}} = \frac{225}{13750} = 0.0164$$

$$V_{23} = I R_{23} = 0.0164 \times 6250 = 102.5$$

$$\therefore I_3 = \frac{V_{23}}{R_3} = \frac{102.5}{12500} = 0.0082 \text{ A} = \underline{8.2 \times 10^{-3} \text{ A}}$$

(b)  $I(1.25) = I_{\infty} (1 - e^{-1.25}) = (8.2 \times 10^{-3})(1 - e^{-1.25}) = \underline{5.84 \times 10^{-3} \text{ A}}$



$$-I_3 R_3 - I_3 R_2 + \mathcal{E}_L = 0$$

$$\frac{dI_3}{dt} + \frac{I_3}{L} (R_2 + R_3) = 0 \quad \therefore \tau = \frac{L}{R_2 + R_3} = \frac{5.35 \text{ mH}}{25000 \Omega} = \underline{2.14 \times 10^{-7} \text{ s}}$$



$$\epsilon_0 - I_1 R_1 - I_2 R_2 = 0$$

$$-I_3 R_3 + L \frac{dI_3}{dt} + I_2 R_2 = 0$$

$$I_1 = I_2 + I_3$$

$$\frac{dI_3}{dt} - \frac{1}{L} \left(R_3 + \frac{R_1 R_2}{R_1 + R_2} \right) I_3 = - \frac{\epsilon_0 R_2}{(R_1 + R_2) L}$$

$$\therefore \tau = \frac{L}{\frac{R_1 R_2}{R_1 + R_2} + R_3} = \underline{3.11 \times 10^{-7} \text{ s}}$$