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**FINAL EXAM**

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**REPORT ALL NUMBERS TO THREE SIGNIFICANT FIGURES!**  
**Use the conversion constants and data given on the front page.**

5 red (a) A diffraction grating has 5000 lines/cm. Laser light of 650 nm (red) is sent through this grating at normal incidence. What is the angle of the second order spot that comes out?

$$2\lambda = d \sin \theta \quad \Rightarrow \quad \sin \theta = \frac{2\lambda}{d} = \frac{2 \times 650 \times 10^{-9}}{\frac{1}{5000} \times 10^{-2}} = 0.65 \quad \theta = 40.5^\circ$$

(b) In a two-slit interference experiment the fifth, tenth, and fifteenth order spots are missing. If the slit separation is 0.275 mm, what is the slit width?

$$\frac{5\lambda}{d} = \frac{1\lambda}{a} \quad d = 5a \Rightarrow a = \frac{1}{5} d = 0.055 \text{ mm}$$

(c) Calculate the critical angle for total internal reflection for a diamond ( $n = 2.40$ ) immersed in water ( $n = 1.33$ ).

$$\sin \theta_c = \frac{n_2 \sin 90^\circ}{n_1} = \frac{1.33}{2.40} = 0.554 \quad \theta_c \approx 33.65^\circ$$

(d) Calculate the polarizing angle for diamond ( $n = 2.40$ ) immersed in water ( $n = 1.33$ ), where the light is incident from the water.

$$\tan \theta = \frac{n_2}{n_1} = \frac{2.4}{1.33} = 1.8 \quad \theta \approx 60.9^\circ$$

2 (e) The intensity of sunlight is observed to be 980 W/m<sup>2</sup> in a plane perpendicular to the light beam. Calculate the peak value of the magnetic field in this light.

$$\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B} \quad WC = \epsilon_0 E^2 C = 980 \frac{\text{W}}{\text{m}^2} = \frac{B^2 C}{\mu_0} \quad B = \sqrt{\frac{980 \times 4\pi \times 10^{-7}}{(3.0 \times 10^8)^2}} = 2.87 \times 10^{-6} \text{ T}$$

$\sin \theta = \frac{10^{-2}}{4.5}$

(f) Laser light of wavelength 550 nm is incident on a single slit. On a screen 4.50 m away the two minima on either side of the center are 2.00 cm apart. Calculate the width of the slit.

$$a \sin \theta = m\lambda \quad a = \frac{\lambda}{\sin \theta} = \frac{550 \times 10^{-9}}{0.07/4.5} = 2.475 \times 10^{-4} \text{ m} \quad 0.2475 \text{ mm}$$

