

SIXTH MIDTERM

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REPORT ALL NUMBERS TO THREE SIGNIFICANT FIGURES!

Use the conversion constants and data given on the front page.

- (a) A two-slit interference pattern is projected on a screen 3.50 cm from the slits using a laser light of wavelength 525 nm. If the slits are 0.200 mm apart and are very narrow, find the distance between the $m = 0$ and $m = 1$ maxima.

$$a \sin \theta = m \lambda$$

$$\Delta y = L \tan \theta \quad \left. \begin{array}{l} \sin \theta \approx \tan \theta \\ \Delta y = L \frac{m \lambda}{a} = 3.50 \text{ cm} \times \frac{1 \times 525 \times 10^{-9} \text{ m}}{0.2 \times 10^{-3} \text{ m}} = 9.19 \times 10^{-3} \text{ cm} \end{array} \right\}$$

- (b) A single slit of width 0.050 mm is illuminated with light of 525 nm as above. The distance from slit to screen is 3.50 m. Calculate the distance on the screen between the $m = +1$ and $m = -1$ minima.

$$a \sin \theta = m \lambda \quad \sin \theta = \frac{m \lambda}{a} = \frac{2 \times 525 \times 10^{-9} \text{ m}}{0.05 \times 10^{-3} \text{ m}} = 0.0210 \quad \theta = 1.20^\circ$$

$$\Delta y = L \tan \theta = 3.50 \text{ m} \times \tan 1.20^\circ = 0.0735 \text{ m} = 7.35 \times 10^{-2} \text{ m}$$

- (c) White light is incident perpendicular on a soap film ($n = 1.34$) of thickness 0.750×10^{-6} m. Calculate ALL the wavelengths in the visible (400 nm to 700 nm) that show constructive interference in reflection.

$$2nd = (k + \frac{1}{2}) \lambda \quad 2 \times 1.34 \times 0.750 \times 10^{-6} \text{ m} = (k + \frac{1}{2}) \lambda \quad \lambda = \frac{2010 \text{ nm}}{k + \frac{1}{2}}$$

$k=1: \lambda = 1340 \text{ nm}$	$k=4: \lambda = 447 \text{ nm}$	} The visible wavelengths are: 574 nm, 447 nm
$k=2: \lambda = 804 \text{ nm}$	$k=5: \lambda = 365 \text{ nm}$	
$k=3: \lambda = 574 \text{ nm}$	\vdots	

- (d) Determine the critical angle for total internal reflection for diamond ($n = 2.40$) immersed in water ($n = 1.34$)

$$\sin \theta_c = \frac{n_{\text{water}}}{n_{\text{diamond}}} = \frac{1.34}{2.40} = 0.558 \quad \theta_c = 33.9^\circ$$

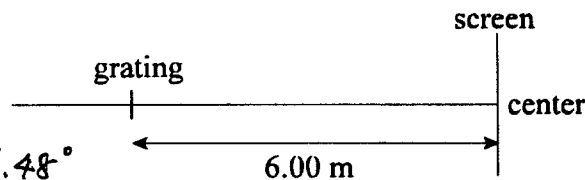
- (e) Find the polarizing angle for light incident on a diamond under water.

$$\tan \theta_p = \frac{n_{\text{diamond}}}{n_{\text{water}}} = \frac{2.40}{1.34} = 1.79 \quad \theta_p = 60.8^\circ$$

- (f) For a diffraction grating with 75.0 lines/mm, calculate the distance from the center for green light ($\lambda = 500 \text{ nm}$) in 3rd order.

$$d = \frac{1 \text{ mm}}{75.0 \text{ lines}} = 0.0133 \text{ mm} = 1.33 \times 10^{-5} \text{ m}$$

$$\sin \theta = \frac{m \lambda}{d} = \frac{3 \times 500 \times 10^{-9} \text{ m}}{1.33 \times 10^{-5} \text{ m}} = 0.113 \quad \theta = 6.48^\circ$$



$$\Delta y = L \tan \theta = 6.00 \text{ m} \times \tan 6.48^\circ = 0.68 \text{ m}$$